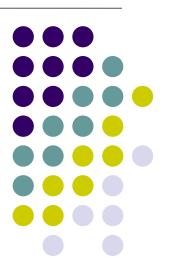
Applied Scaling & Classification Techniques in Political Science

Lecture 5

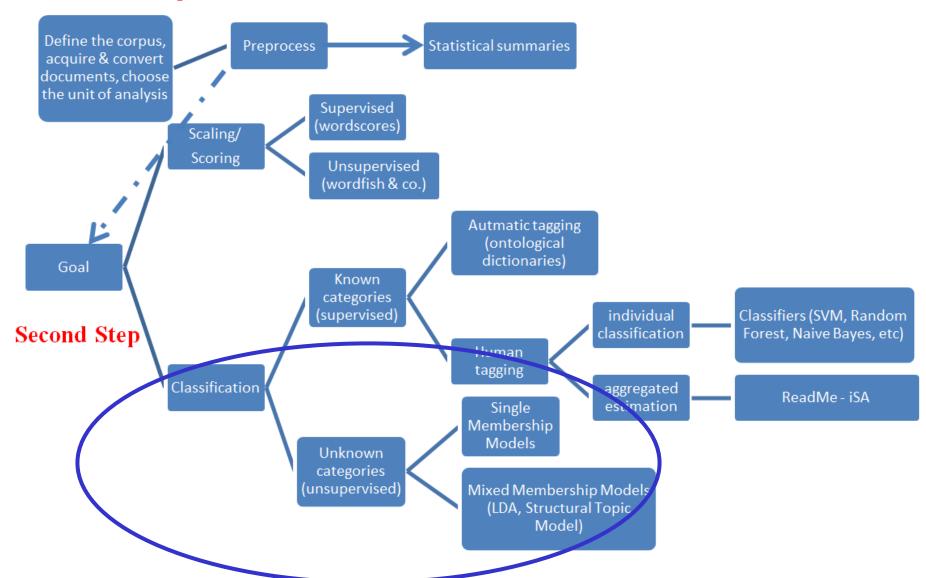
Unsupervised classification methods: the structural topic model



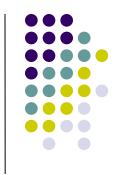
Our Course Map



First Step







- ✓ Roberts, Margaret E., Brandon M. Stewart, Dustin Tingley, Christopher Luca, Jetson Leder-Luis, Shana Kushner Gadarian, Bethany Albertson, David G. Rand (2014). Structural Topic Models for Open-Ended Survey Response, *American Journal of Political Science*, 58(4), 1064-1082
- ✓ Roberts, Margaret E., Brandon M. Stewart, Dustin Tingley(2014). STM: R Package for Structural Topic Models, *Journal of Statistical Software*, https://cran.rproject.org/web/packages/stm/vignettes/stmVignette.pdf

that

Scaling methods differs from classification methods in that scaling aims to estimate a **position** on a latent dimension, while classification aims to estimate a **text's membership in a latent class**...more in details...

Classification methods organize texts into a set of known (or unknown) categories





Sometimes researchers know the categories beforehand

In this case, the challenge is to attribute a semantic meaning to each text in a corpus given a **precoded set** of words (or texts) that have been already assigned to some categories (this is why such way of classification is called "supervised")

This step is also called *tagging*, and tagging may occur through *automatic* (via a **dictionary** for example) or *human* coding

Machine learning algorithms, as we will see, can be considered as supervised classification methods



- Classification methods can also be used to **discover new** ways of organizing texts
- Unsupervised classification methods are a class of methods that "learn" underlying features of text without explicitly imposing categories of interest (as it happens with supervised methods)
- They use modeling assumptions and properties of the texts to estimate a **set of categories** and simultaneously **assign documents (or parts of documents)** to those categories
- Therefore such models *infer* rather than *assume* the content of the categories under study

Back to validation

- Because text analysis methods are necessarily incorrect models of language (remember!), the output always necessitates careful validation
- For **supervised classification methods**, this requires demonstrating that the classification from machines replicates hand-coding
- For unsupervised classification and scaling methods, this requires validating that the measures produced correspond with the concepts claimed





- Supervised and unsupervised methods are different models with different objectives
- If there are **predetermined categories** and documents that need to be placed in those categories, then use a supervised learning method!
- If, however, researchers approach a problem without a **predetermined categorization scheme**, unsupervised methods can be useful. Supervised methods will never contribute a new coding scheme by definition!

Far from being competitors, supervised and unsupervised methods can *then* be productively viewed as **complementary methods**, particularly for new projects

For example, the categories of interest in a new corpus can be unclear or could benefit from extensive exploration of the data. In this case, unsupervised methods provide insights into classifications that would be difficult to obtain without guidance

Once the unsupervised method is fit, supervised learning methods can be used to validate or generalize the findings

Among the unsupervised classification methods, we can have...

Single membership models: these technique aims to rearrange observations (i.e., documents in a corpus) into homogenous groups according to some notion of distance among them

That's the idea of a clustering!

The clustering of documents into k groups is done in way that **maximises** the differences between groups and **minimises** the differences within them

These groups are not labelled (it is an unsupervised method of classification after all!), and so they must be interpreted ex post based on a reading of their content or the association of the documents with some known external categories

More in details...

....given a **dissimilarity measure** *d* among the documents (for example, Euclidean distance: we already discussed about it in Lecture 1!), *clustering* algorithms proceed by grouping (*agglomerative* methods) or splitting (*dissociative* methods) subsequently the whole set of data according to *d*

If this procedure is sequential, the method is called hierarchical

For example, an **agglomerative hierarchical method** is as follows: a first group is formed by taking the closest units in the data (according to *d*), where that difference is measured as their squared Euclidean distance in the features space

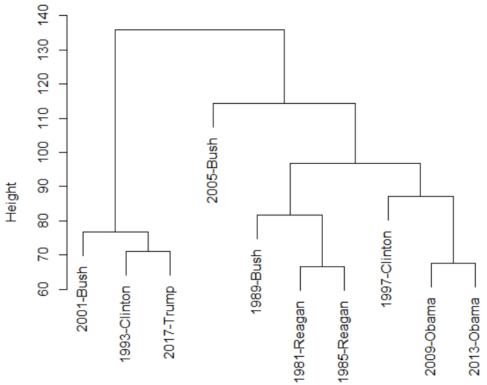
Then each new aggregation occurs either forming a new group of two units, or aggregating a unit to the closets group already formed or aggregating two distinct groups

An example from the Inaugural Speeches by US Presidents corpus

The hierarchical agglomerative cluster algorithm works as follows:

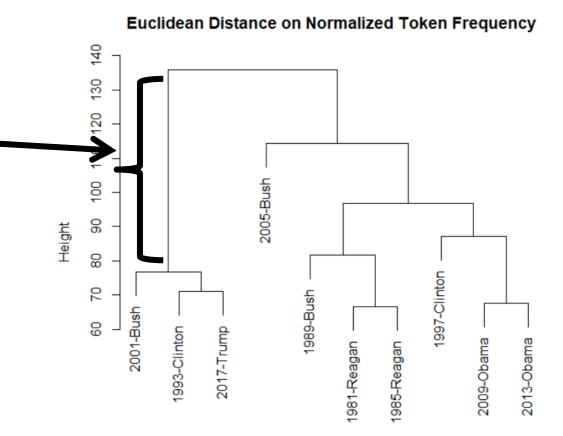
- 1) Put each document in its own cluster
- 2) Identify the closest two clusters and combine them into one cluster
- 3) Repeat the above step till all the documents are in a single cluster

Euclidean Distance on Normalized Token Frequency



An example from the Inaugural Speeches by US Presidents ¢orpus

In the **dendrogram**, long vertical lines indicate more distinct separation between the groups, while short vertical bars show observations that are all close to each other







The main limit of the **single membership model** approach is that it operates from an assumption that each document must belong to a category and that categories do not overlap

This setting could result as too restrictive when classifying more complex documents, such as political speeches

In this case, each politicians' speech is likely to deal with a variety of categories





Mixed membership models (aka, topic models) assume precisely that each document is a mixture of categories (topics), meaning that a single document can be composed of multiple categories

A non-technical resume

Topic models provide a relatively simple, parametric model describing the relationship between **clusters of co-occurring words representing "topics"** and their relationship to documents which contain them in **relative proportions**

By estimating the parameters of this model, it is possible to recover these topics (and the words that they comprise) and to estimate the degree to which documents pertain to each topic

The **estimated topics are unlabelled**, so a human must assign these labels by interpreting the content of the words most highly associated with each topic, perhaps assisted by contextual information

No human input is required to fit the topics besides a document-feature matrix, with one critical exception: the number of topics must be decided in advance

In fitting and interpreting topic models, therefore, a core concern is choosing the "correct" number of topics. There are statistical measures, but a better measure is often the interpretability of the topics







To understand topic models, we need to start first of all with a better understanding of what we mean by "topic"

Substantively, topics are distinct concepts

In congressional speech, one topic may convey attention to America's involvement in Afghanistan, with a **high probability attached to words** like troop, war, taliban, and Afghanistan

A second topic may discuss the health-care debate, regularly using words like health, care, reform, and insurance

Statistically, a topic is defined as a (multinomial) distribution over the words in the vocabulary of the corpus





- How to estimate a topic (which, remember, is **learned & discovered** rather than **assumed** by the researcher)?
- We can observe **only documents and words**, **not topics** the latter are part of the hidden (or latent)
 structure of documents
- Still, our aim is to infer precisely the latent topic structure given the words and document
- For solving this riddle, models use the patterns of words co-occurrence within and across documents





To this aim, we can for example taking advantage of the Latent Dirichlet Allocation (LDA) model

The basic assumption behind LDA is that each of the documents in a corpus consists of a **mixture of topics** (by "mixture" in this context we mean a set of positive values that sum to one), with **each word** within a given document belonging to **exactly one topic**

Moreover each word is assumed to be conditionally independent given its topic





As a result, each document can be represented as a vector of proportions that denote what fraction of the words belongs to each topic

Documents, then, are a **probability distribution over topics**. In this sense, a whole document may be "classified" into a given topic, but more accurately portions of documents are classified into topics across the entire corpus

In single membership models, on the contrary, **each document is restricted to only one topic (i.e., group)**, so all words within it are generated from the same distribution





- LDA "recreates" the documents in the corpus by adjusting the relative importance of topics in documents and words in topics **iteratively**, that is...
- ...given a corpus, LDA **backtracks** and tries to figure out what topics would create the documents included in the corpus in the first place!





The assumed **data generating process** for each document is as follows:

Let's suppose you have *N* documents in your corpus and the total number of words (features) in your document-term-matrix is *M*

You begin by telling to the algorithm how many topics (*K*) you think there are in your corpus. You can either use an informed estimate (e.g. results from a previous analysis), or simply trial-and-error (more on this later on)





LDA then splits the original TDM of our corpus into two lower dimensions matrices (an example with *K*=2)

	w1	w2	w3	wm
d1	0	2	3	1
d2	2	0	2	4
dn	3	1	2	3

	k1	k2
d1	??	??
d2	??	??

	w1	w2	w3	wm
k1	??	??	??	??
k2	??	??	??	??

This is a document-topics matrix with

dimension (N, K)

N = total number of documents (d)

K = total number of topics (k)

M = the vocabulary size (words: w)

This is a **topic-terms matrix** with dimension (K, M)

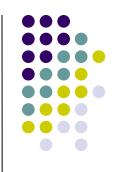




A **topic mixture** $\theta_{d,k}$ is then drawn for the document d according to a Dirichlet distribution over the fixed set of K topics (say K=3, $\theta_{d,k}$ = 0.3, i.e., 30% of the words in document d refers to topic 1; 0.4; 0.4)

Dirichlet distributions provide good approximations to word distributions in documents and are computationally convenient





The **probability** of observing a word in the vocabulary under a certain topic ($\beta_{k,w}$) is then given by a two-step process:

- a) the first step is to draw the topic;
- b) conditional on topic assignment, the actual word is drawn from a multinomial distribution





Each w word in a document d is assigned only to one topic. However, if a word **appears twice** in a document, each word may be assigned to different topics

LDA considers that any given topic will have a **high** probability of generating certain words and a low probability of generating other words



After having defined the total number of topics K to discover, LDA starts with some given values for $\theta_{d,k}$ and $\beta_{k,w}$

This first assignment already gives you both topic representations of all the documents and word distributions of all the topics (albeit not necessarily a very good ones)

So to improve on them, **both values are updated** throughout the LDA process in the following way:

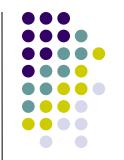
for each document d...

....go through each word w in d...

- ...and for each topic *k*, compute two things:
- p(topic k | document d) = the proportion of words in document d that are currently assigned to topic k, i.e., how prevalent are topics in the document?
- 2) p(word w | topic k) = the proportion of assignments to topic k over all documents that come from this word w, i.e., how prevalent is that word across topics?

What we mean by that? An example





Imagine you are analyzing **two documents** about foods and animals with the following words:

Document X	Document Y
Fish	Fish
Fish	Fish
Eat	Milk
Eat	Kitten
Vegetables	Kitten

You select at the beginning K=2 (let's label these two topics as F and P as an example)



Suppose that the initial random distribution after the first assignment done by LDA is the one that appears below

	Document X		Document Y
F	Fish	Р	Fish
F	Fish	F	Fish
F	Eat	F	Milk
F	Eat	Р	Kitten
F	Vegetables	Р	Kitten

Imagine now that we are now checking the possible **new**topic assignment for the word "fish" in Doc Y.

Assuming that all topic assignments except for the current word in question, are correct, changing the topic assignment of word "fish" in Doc Y from topic P to topic F, is going to improve the model or not?

	Document X		Document Y
F	Fish	?	Fish 😽
F	Fish	F	Fish
F	Eat	F	Milk
F	Eat	Р	Kitten
F	Vegetables	Р	Kitten





How prevalent are topics in the document? Since the words in Doc Y are assigned to Topic F and Topic P in a 50-50 ratio, the remaining "fish" word seems equally likely to be about either topic.

	Document X		Document Y
F	Fish	?	Fish
F	Fish	F	Fish
F	Eat	F	Milk
F	Eat	Р	Kitten
F	Vegetables	P	Kitten





How prevalent is that word across topics? The "fish" words across both documents appears nearly half of the time in Topic F words (3/7), but 0% among Topic P words

	Document X		Document Y
F	Fish	?	Fish
F	Fish	F	Fish
F	Eat	F	Milk
F	Eat	Р	Kitten
F	Vegetables	Р	Kitten

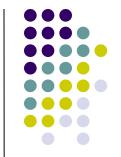




As a conclusion from the two criteria (i.e., by multiplying the two previous probabilities), we would move the "fish" word of Doc Y to Topic F

Doc Y might then be a document on "what to feed kittens"?

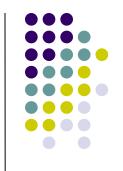




By following this procedure, we (eventually) reassign w' to a new topic, where topic k is chosen with probability p(topic k | document d) * p(word w | topic k)

According to our generative model, this is essentially the probability that topic k generated word w

When doing it, we are assuming that all topic assignments except for the current word in question, are correct, and then we update the assignment of the current word using our model of how documents are generated



After repeating the previous step a large number of times, you'll eventually reach a roughly steady state where your assignments (the document topic and topic term distributions) are pretty good

This is the **convergence point** of LDA

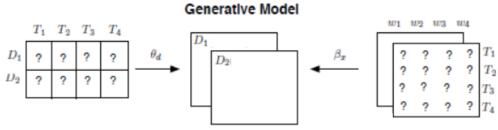
LDA uses a process known as *collapsed Gibbs sampling*: Gibbs sampling works by performing a random walk in such a way that reflects the characteristics of a desired distribution (in our case, the Dirichlet one). The starting point of the walk is chosen at random

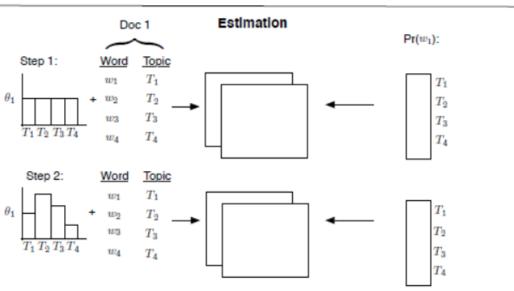


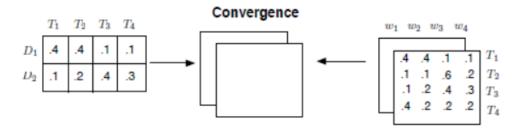
Once the convergent point is reached, use the obtained assignments to estimate the:

- 1. **Document-topic proportions** (by counting the proportion of words assigned to each topic *within* that document)
- 2. Topic-word proportions (by counting the proportion of words assigned to each topic overall, i.e., across documents)

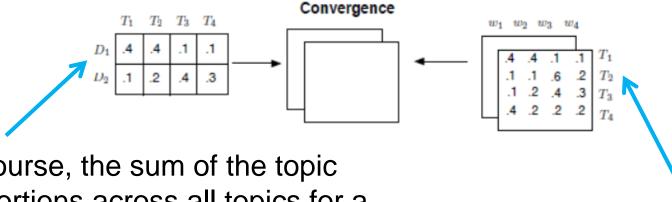










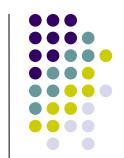


Of course, the sum of the topic proportions across all topics for a document is 1

Of course, the sum of the topic probabilities for a word, across all topics, is 1

Going back to our example

Document X		Document Y
Fish		Fish
Fish		Fish
Eat		Milk
Eat		Kitten
Vegetables		Kitten



	fish	eat	vegetables	milk	kitten
D1	2	2	1	0	0
D2	2	0	0	1	2

	K1	K2
D1	?	?
D2	?	?

	fish	eat	vegetables	milk	kitten
K1	?	?	?	?	?
K2	?	?	?	?	?

Document-topics matrix

Topic-terms matrix

Going back to our example (where K1=F; K2=P)

	fish	eat	vegetables	milk	kitten
D1	2	2	1	0	0
D2	2	0	0	1	2

	fish	eat	vegetables	milk	kitten
D1	2 (F)	2 (F)	1 (F)	0	0
D2	2 (F)	0	0	1 (F)	2 (P)

	K1	K2
D1	1	0
D2	0.6	0.4

	fish	eat	vegetables	milk	kitten
K1	0.5	0.25	0.125	0.125	0
K2	0	0	0	0	1

Document-topics matrix

Topic-terms matrix





The quantities of interest from a Topic Model:

QOI: Document-Topic Proportions

- Level of Analysis: Document
- Part of the Model: θ
- Description: Proportion of words in a given document about each topic.
- Example Use: Can be used to identify the documents that devote the highest or lowest proportion of words to a particular topic. Those with the highest proportion of words are often called "exemplar" documents and can be used to validate that the topic has the meaning the analyst assigns to it.





The quantities of interest from a Topic Model:

QOI: Topic-Word Proportions

- Level of Analysis: Corpus
- Part of the Model: κ, β
- Description: Probability of observing each word in the vocabulary under a given topic. Alternatively, the analyst can use the FREX scoring method
- Example Use: The top 10 most probable words under a given topic are often used as a summary of the topic's content and help inform the user-generated label.

The challanges of any topic model:

1. Understanding the semantic meaning of a topic

A **semantically interpretable topic** has two qualities:

(a) it is *coherent/cohesive* in the sense that high-probability words for the topic tend to co-occur (i.e., *do top words* of one topic tend to co-occur across documents?)

Therefore semantic coherence is a property of the "within topics"

Semantic coherence **however** only addresses whether a topic is internally consistent (i.e., it checks if we are evaluating a well-defined concept)

It does not penalize topics that are alike

This could be a problem!



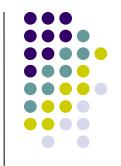
The challanges of any topic model:

1. Understanding the semantic meaning of a topic

A semantically interpretable topic has two qualities

(b) it is *exclusive* in the sense that the top words for that topic are unlikely to appear within top words of other topics (i.e., *are the top words of one topic different from the top words of other topics*?): if words with high probability under topic *k* have low probabilities under other topics, then we say that topic *k* is exclusive

Therefore semantic exclusivity is a property of the "between topics"



The challanges of any topic model:

- 1. Understanding the semantic meaning of a topic
- A topic that is both *cohesive and exclusive* is more likely to be **semantically useful**
- The frequency/exclusivity (**FREX**) scoring summarizes words according to their probability of appearance under a topic and the exclusivity to that topic
- These words provide more semantically intuitive representations of each topic

The challanges of any topic model:

2. How many topics?

The analyst **must choose the number of topics**. There is no "right" answer to this choice. Varying the number of topics varies the level of granularity of the view into the data

Therefore, the choice will be dependent both on the nature of the documents under study and the goals of the analysis

The appropriateness of particular levels of aggregation will vary with your research question

Given that is practically impossible to guess the exact number of topics in the corpus (although new empirically tests have been introduced in the literature...), a good practice is beginning with a wider number of topics rather than a potentially too narrow one

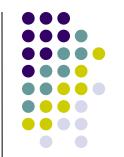
Then a researcher should settled on a specification of *K* lower that the initial one when she found that at higher specifications, substantively-meaningful topics were being divided up in ways that were less amenable to testing her hypotheses

Largely, the answer will be related to the **semantic meaning** of the topics extracted. The researcher is tasked with selecting any number of topics (K) and confirming that those recovered are **substantively meaningful**!!!

Examining the terms with highest probabilities of belonging to each topic and reading the documents with highest probabilities of belonging to it gives the researcher a sense of the substantive meaning of each topic

In practice the precise choice of topics contains a degree of **arbitrariness**, and often to recover interpretable topics, some extra ones are also generated that are not readily interpretable





Structural Topic Model (STM) innovates on the models just described in two different ways:

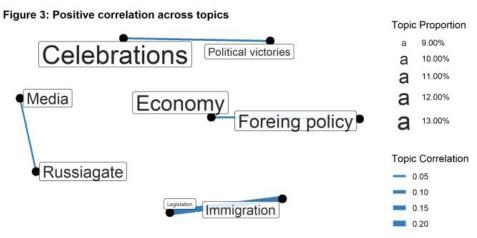
First: topic proportions $(\theta_{d,k})$ are allowed to be **correlated**: this is a reasonable assumption given that in documents topics discussed are correlated!

For example, if a manifesto contains discussion of Topic X (e.g. administrative reform), the probabilities that it will also contain discussion of Topics Y (e.g. curbing public works) and Z (e.g. reducing the number of Lower House members), are not independent of each other, but correlated

In this sense, STM fits a Correlated Topic Model (rather than a LDA)

Graphical depictions of the correlation between topics provide insight into the organizational structure at the corpus level

In essence, the model identifies when two topics are likely to co-occur (by focusing on positive correlation) within a document



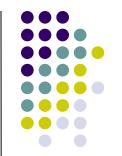


Structural Topic Model (STM) innovates on the models just described in two different ways:

Second: in all topic models, the analyst estimates for each document the proportion of words attributable to each topic, providing a measure of *topic prevalence*. The model also calculates the words most likely to be generated by each topic, which provides a measure of *topical content*

However, in standard LDA, the document collection is assumed to be **unstructured**; that is, each document is assumed to arise from the same data-generating process irrespective of additional information the analyst might possess





By contrast, a STM framework is designed to incorporate additional information about the document or its author into the estimation process

That is, rather than assuming that **topical prevalence** (i.e., the frequency with which a topic is discussed) and **topical content** (i.e., the words used to discuss a topic) **are constant** across all documents, the analyst can incorporate covariates over which we might expect to see variance

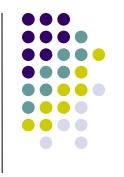
This allows to measure **systematic changes** in topical prevalence and topical content over the conditions in our experiment, as measured by the *X* covariates for prevalence and the *U* covariates for content

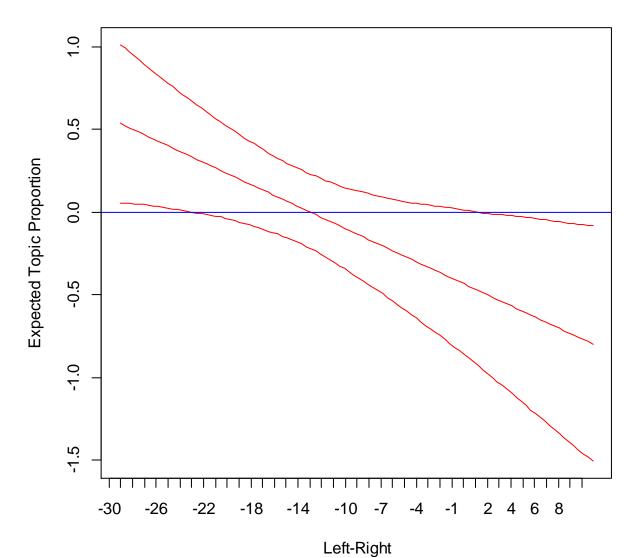
Thus, for example, we can easily obtain measures of how our treatment condition affects how often a topic is discussed (prevalence)!

➢ for example, do documents of left parties discuss more about a given topic than documents of right parties?

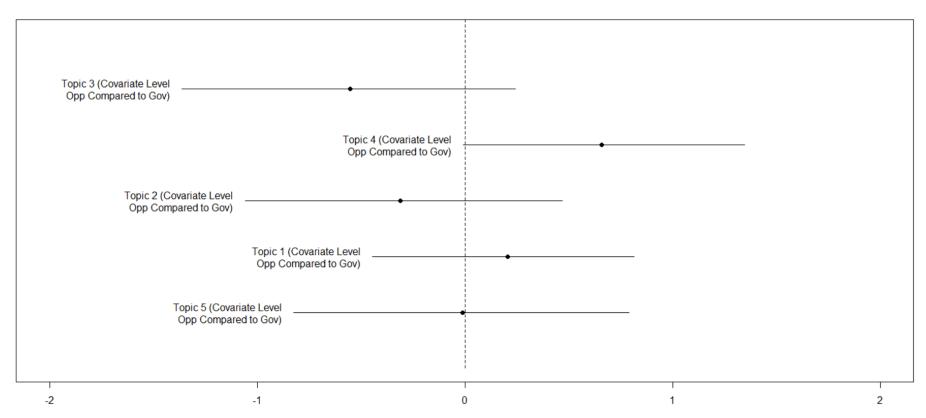


Topic 4: over LR









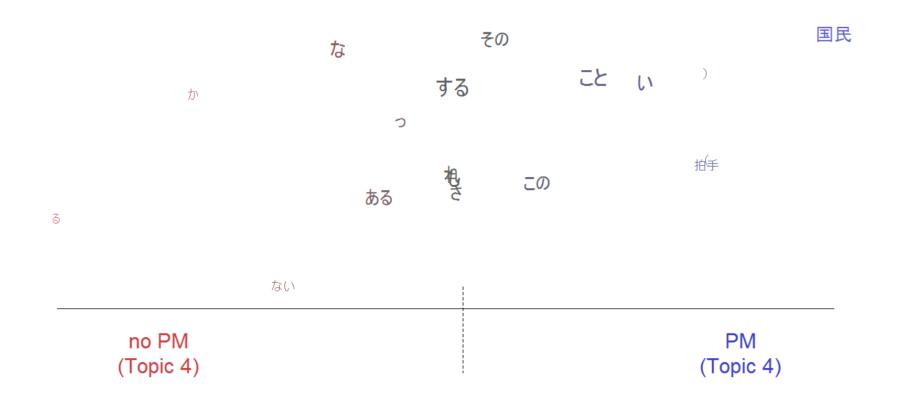
Reported coefficient: «opposition – government»





- Moreover, we can easily obtain measures of how the language used to discuss the same topic (content)
- for example, when men politicians discuss about a particular topic do they use the same words than female politicians?









STM conducts this type of analysis, while **simultaneously** estimating the topics

This is more efficient than doing the two processes in separated steps: aka, first the topic analysis, and then running an analysis on the topic extracted

- In the STM framework, the researcher has therefore the option to choose covariates to incorporate in the model
- These covariates inform either the **topic prevalence** or the **topical content** latent variables with observed information about the respondent
- The analyst will want to include a covariate in the topical prevalence portion of the model (*X*) when she believes that the observed covariate will affect *how much* the respondent is to discuss a particular topic
- The analyst also has the option to include a covariate in the topical content portion of the model (*U*) when she believes that the observed covariate will affect *the words* which a respondent uses to discuss a particular topic







These two sets of covariates can overlap, suggesting that the topic proportion and the way the topic is discussed change with particular covariate values





The quantities of interest from a **Structural** Topic Model (beyond the previous two...)

QOI: Topical Prevalence Covariate Effects

- Level of Analysis: Corpus
- Part of the Model: θ, X
- Description: Degree of association between a document covariate X and the average proportion of a document discussing each topic.
- Example Finding: Subjects receiving the treatment on average devote twice as many words to Topic 2 as control subjects.





The quantities of interest from a **Structural** Topic Model (beyond the previous two...)

QOI: Topical Content Covariate Effects

- Level of Analysis: Corpus
- Part of the Model: κ, U
- Description: Degree of association between a document covariate U and the rate of word use within a particular topic.
- Example Finding: Subjects receiving the treatment are twice as likely to use the word "worry" when writing on the immigration topic as control subjects.

STM and R

install.packages("topicmodels", repos='http://cran.us.rproject.org')

If you have any problems to install the package «stmBrowser», please download it <u>from here</u>, and install it on R as «local files»

